

(\* RSA (Rivest-Shamir-Adleman) cryptosystem  
Firstly we will encrypt a credit card number 5613  
7024 3798 6943 by the public key (n,e). Secondly we will  
find a private key d and decrypt the credit card number. \*)

In[11]:= (\* public key \*)  
n := 1000001;  
e := 13;

In[13]:= (\* prime factorization of n \*)  
FactorInteger[n]

Out[13]= {{101, 1}, {9901, 1}}

In[18]:= (\* n=pq \*)  
p := 101;  
q := 9901;

In[20]:= (\* L \*)  
L := LCM[p - 1, q - 1];  
L

Out[21]= 9900

(\* prime factorization of L \*)  
FactorInteger[L]

Out[22]= {{2, 2}, {3, 2}, {5, 2}, {11, 1}}

(\* de-kL=1 \*)  
{g, {d, k}} = ExtendedGCD[e, L]

Out[24]= {1, {-1523, 2}}

In[26]:= (\* d \*)  
d := -1523 + L  
d

Out[27]= 8377

(\* encryption of 5613 7024 3798 6943\*)  
Mod[{5613 ^ e, 7024 ^ e, 3798 ^ e, 6943 ^ e}, n]

Out[28]= {675406, 911491, 446624, 644570}

In[30]:= (\* decryption of 675406 911491 446624 644570 \*)  
Mod[{675406 ^ d, 911491 ^ d, 446624 ^ d, 644570 ^ d}, n]

Out[30]= {5613, 7024, 3798, 6943}

