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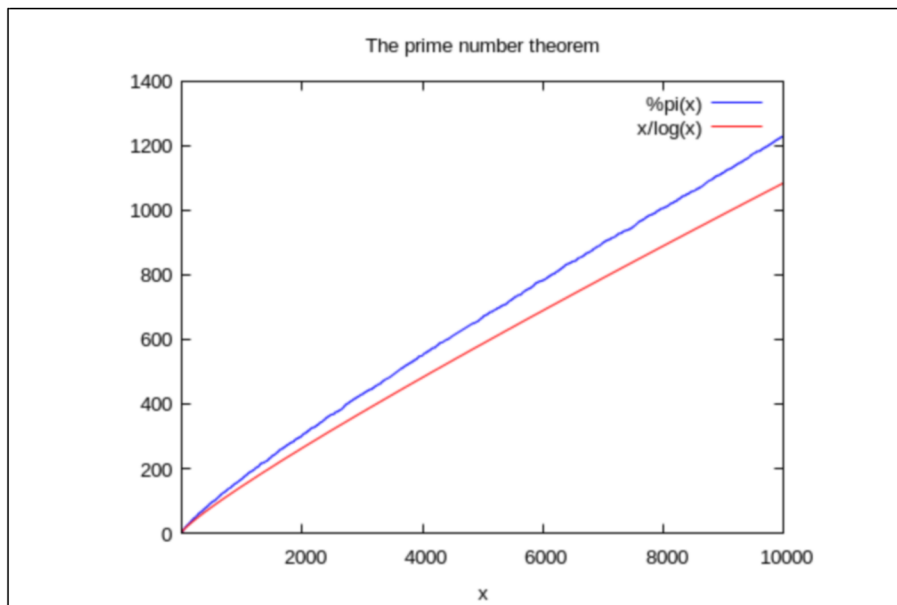
(%i1) pi1[n]:=if n<2 then 0 elseif primep(n) then pi1[n-1]+1 else pi1[n-1];
(%o1) pi1_n:=if n<2 then 0 elseif primep(n) then pi1_{n-1}+1 else pi1_{n-1}

(%i2) / . Define  $\pi(x)$  = the number of primes less than or equal to  $x$  . /
pi(x):=if integerp(x) and primep(x) then pi1[x]-1/2 else pi1[floor(x)];
(%o2) pi(x):=if integerp(x)  $\wedge$  primep(x) then pi1_x -  $\frac{1}{2}$  else pi1_{floor(x)}

(%i4) / . The graphs of  $\pi(x)$  and  $x/\log(x)$ 
The prime number theorem shows that
 $\pi(x)/(x/\log(x)) \rightarrow 1$  as  $x \rightarrow \infty$  . . /
wxplot2d([pi(x), x/log(x)],
[x,1.5,10000], [xtics,2000],
[legend," $\pi(x)$ ", "x/log(x)"],
[title,"The prime number theorem"]);

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(%t4)



(%o4)