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→ / · RSA (Rivest-Shamir-Adleman) cryptosystem
Firstly we will encrypt a credit card number
5613 7024 3798 6943 by the public key (n,e)
Lastly we will find a private key d and decrypt the number.
· /

→ / · public key n=1000001, e=13 · /;

(%i1) / · factorization of n · /
      factor(1000001);
(%o1) 101 9901

(%i2) / · L · /
      lcm(100,9900);
(%o2) 9900

(%i3) / · factorization of L · /
      factor(9900);
(%o3) 22 32 52 11

(%i4) / · gcd(L,e)=1? · /
      gcd(9900,13);
(%o4) 1

(%i5) / · Load a function finding a solution (d,k) to de-kL=1. · /
      load(gcdex)$

(%i6) / · Find a private key d. · /
      igcdex(13,9900);
(%o6) [-1523, 2, 1]

(%i7) / · Find a private key d which is the minimum positive integer. · /
      -1523+9900;
(%o7) 8377

(%i8) / · encryption of plaintext 5613 · /
      mod(5613^13,1000001);
(%o8) 675406

(%i9) / · decryption of ciphertext 675406 · /
      mod(675406^8377,1000001);
(%o9) 5613

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(%i10) / . encryption of plaintex 7024 . /  
      mod(7024^13,1000001);  
(%o10) 911491  
  
(%i11) / . decription of ciphertext 911491 . /  
      mod(911491^8377,1000001);  
(%o11) 7024  
  
(%i12) / . encription of plaintex 3798 . /  
      mod(3798^13,1000001);  
(%o12) 446624  
  
(%i13) / . decription of ciphertext 446624 . /  
      mod(446624^8377,1000001);  
(%o13) 3798  
  
(%i14) / . encription of plaintex 6943 . /  
      mod(6943^13,1000001);  
(%o14) 644570  
  
(%i15) / . decription of ciphertext 644570 . /  
      mod(644570^8377,1000001);  
(%o15) 6943
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